## HW one, MTH 418, Spring 2016

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QUESTION 1. (i) Let $V=\{2,4,5,6,8\} \subset Z_{10}$. Two vertices $v_{1}, v_{2} \in V$ are connected by an edge iff $v_{1} * v_{2}=0$ (* $^{*}$ here means multiplication module 10). Construct such graph. Is it a $B_{n, m}$ for some $n, m$ ? Find the Girth and the diameter of the graph.
(ii) Let $V=\{3,5,6,9,10,12\} \subset Z_{15}$. Two vertices $v_{1}, v_{2} \in V$ are connected by an edge iff $v_{1} * v_{2}=0$ (* here means multiplication module 15). Construct such graph. Is it a $B_{n, m}$ for some $n, m$ ? Find the Girth and the diameter of the graph.
(iii) Let $V=\{0,1,2,3,4,5,6,7\}=Z_{8}$. Two vertices $v_{1}, v_{2} \in V$ are connected by an edge iff $v_{1}+v_{2} \in\{0,2,4,6\}$. (note that + here means addition module 8). Construct such graph. Show that the graph is not connected. What is $d\{3,1\}$ ? What is $d(1,4)$ ?. Show that the graph is the union of two disjoint subgraphs, $G_{1}, G_{2}$ such that each $G_{i}$ is a complete induced subgraph.
(iv) Let $V=\{0,1,2,3,4,5,6,7,8\}=Z_{9}$. Two vertices $v_{1}, v_{2} \in V$ are connected by an edge iff $v_{1}+v_{2} \in\{0,3,6\}$. (note that + here means addition module 9). Construct such graph. Show that the graph is not connected. What is $d\{3,2\}$ ? What is $d(5,8)$ ? Show that the graph is the union of two disjoint subgraphs, $G_{1}, G_{2}$ where $G_{1}$ is a complete induced subgraph and $G_{2}=B_{n, m}$ for some $n, m$ is also an induced subgraph.

## Due date: Thursday at noon Feb 18,2016 Faculty information

